
How to Value a Seasonal Company's Discounting Cash Flows

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Abstract:

The correct way of valuing seasonal companies by cash flow discounting is to use monthly data. We may use annual data, but it requires some adjustments. We show that when using annual data in the context of the adjusted present value (APV), the value of the unlevered equity (V_u) and the value of the tax shields (VTS) calculations must be adjusted. However, the debt that we have to subtract to calculate the equity value does not need to be adjusted. We derive the adjustments to be made. Errors due to using annual data without doing the adjustments are big. To adjust only by using average debt and average working capital requirements does not provide a good approximation.

When the inventories are a liquid commodity such as grain or seeds, it is not correct to consider all of them as working capital requirements. The excess inventories financed with debt are equivalent to a set of futures contracts. We show that not considering it undervalues the company.

This paper values a company in which the seasonality is due to the purchases of raw materials: the company buys and pays all raw materials in the month of December. We show that the equity value calculated using annual data without doing the adjustments understates the true value in a 45% if the valuation is done at the end of December, and overstates the true value in a 38% if the valuation is done at the end of November. The error of adjusting only by using average debt and average working capital requirements ranges from -17.9% to 8.5%.

Key Words: Valuation of Seasonal Companies, Seasonality, Cash Flow Discounting

JEL Classification: G12, G31, M21

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1. Introduction

Little attention has been paid to the impact of seasonality on the valuation of companies. Damodaran (1994), Brealey and Myers (2000), Penman (2001), and Copeland (2000) do not even include the terms “seasonal” or “seasonality” in their indexes.

We may define seasonality of cash flows as the variance of the monthly cash flows of a company. We normally say that a company exhibits a seasonality pattern when the variance of the monthly cash flows is high.

Seasonality normally is due to sales (as in the case of toy factories), to purchases (as in the case of edible oil producers) or to production decisions. When valuing companies, seasonality affects the calculation of the Free Cash Flows through the increase of Working Capital Requirements.

When valuing seasonal companies using annual data (instead of monthly data) it is necessary to make some adjustments. The errors derived of using annual data without adjustments for valuing companies are big.

In this paper we will use the example of Russoil, a company that buys sunflower seeds to produce and sell oil. The sales of sunflower oil are stable along the year, but the company has a policy of buying all its annual needs of seeds in December. Section 1 describes the company and provides the expected monthly balance sheets, P&Ls and cash flows. Section 2 provides the valuation of the company using monthly data. Section 3 values the company using annual data without adjustments and shows that it understates the true value in a 45% if the valuation is done at the end of December, and overstates the true value in a 38% if the valuation is done at the end of November. Sections 3.1 and 3.2 show the adjustments needed to perform a correct valuation using annual data. We define a correct valuation as one that provides the same value as the valuation using monthly data. Section 4 shows that the error of adjusting the annual data only by using average debt and average working capital requirements ranges from -17.9% to 8.5%. Section 5 presents how the valuation should be modified if the company holds excess inventories that are a liquid commodity. We argue that if the inventories are a very liquid commodity, then it is not correct to treat the excess inventories as working capital requirements. We call excess inventories to those over a minimum or safety inventory. When excess inventories are financed with debt, they are equivalent to a set of futures contracts. We point out that to buy futures contracts on a very liquid commodity is identical to buy the commodity borrowing money. Therefore, the debt incurred in the financing of these future contracts should not be considered financial debt in the valuation. That is exactly what Russoil does: buys the seeds in December borrowing money. We show that not considering it undervalues the company between 12% and 14%. Section 6 concludes.

2. Description of Russoil, a Seasonal Company

Russoil is a seasonal company that buys seeds and produces sunflower oil. The seasonality is due to the fact that the seeds are purchased and paid in December. Table 1 shows the projected balance sheets and P&Ls for the first months of the company. The company does not own fixed assets. The company has a policy of having \$140,000 as minimum cash and of canceling the debt at least one month every year.

Sales are expected to grow at a monthly rate of 1% until December 2008. From that moment, sales are expected to remain constant until November 2010 when the company will be liquidated. Cost of sales is 75% of sales. 80% of the cost of sales is the cost of seeds. The remaining 20% is mainly labor costs. General expenses are expected to be 16% of sales. Seeds are paid cash and sales are collected cash. The company has not account receivables nor accounts payable. The company pays 0.5% monthly interest on the debt. Corporate taxes are 40%.

Figure 1 shows the seasonality of the inventories and of the debt. Table 2 contains the expected cash flows of Russoil and figure 2 highlights the seasonality of the free cash flows. The equity cash flow is equal to the dividends paid to the shareholders.

Table 1. Projected balance sheets and P&Ls of Russoil (\$000's)

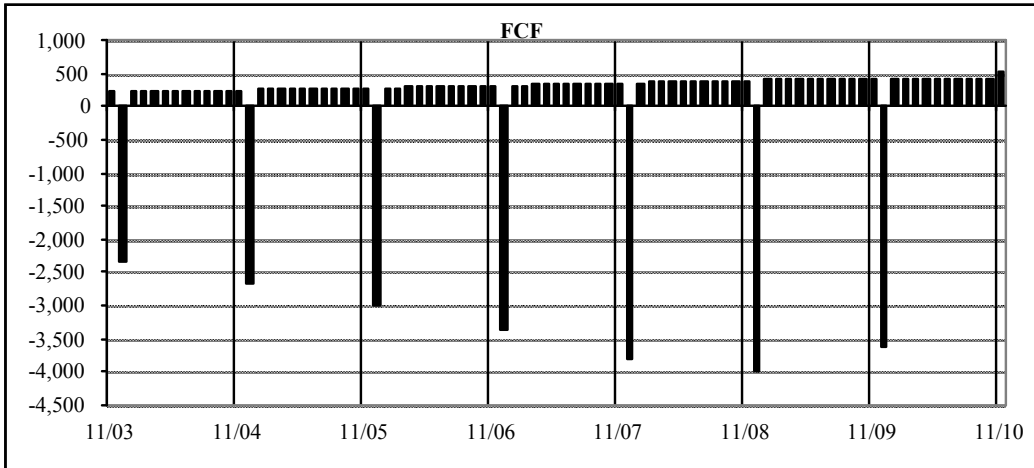
| | 11/03 | 12/03 | 1/04 | 2/04 | 3/04 | 4/04 | 5/04 | 6/04 | 7/04 | 8/04 | 9/04 | 10/04 | 11/04 | 12/04 |
|---------------------|------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|------------|------------|--------------|
| Cash | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 |
| Stocks | 201 | 2,572 | 2,370 | 2,165 | 1,958 | 1,749 | 1,538 | 1,325 | 1,109 | 892 | 672 | 450 | 226 | 2,899 |
| Fixed assets | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| Total assets | 341 | 2,712 | 2,510 | 2,305 | 2,098 | 1,889 | 1,678 | 1,465 | 1,249 | 1,032 | 812 | 590 | 366 | 3,039 |

| | | | | | | | | | | | | | | |
|--------------|------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|------------|------------|--------------|
| Debt | 0 | 2,353 | 2,139 | 1,923 | 1,703 | 1,480 | 1,255 | 1,026 | 794 | 560 | 322 | 81 | 0 | 2,652 |
| Equity | 341 | 359 | 370 | 382 | 395 | 409 | 423 | 439 | 455 | 472 | 490 | 509 | 366 | 387 |
| Total | 341 | 2,712 | 2,510 | 2,305 | 2,098 | 1,889 | 1,678 | 1,465 | 1,249 | 1,032 | 812 | 590 | 366 | 3,039 |

| | | | | | | | | | | | | | |
|---------------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Sales | 334.7 | 338.0 | 341.4 | 344.8 | 348.3 | 351.8 | 355.3 | 358.8 | 362.4 | 366.1 | 369.7 | 373.4 | 377.1 |
| Cost of sales | 251.0 | 253.5 | 256.1 | 258.6 | 261.2 | 263.8 | 266.5 | 269.1 | 271.8 | 274.5 | 277.3 | 280.1 | 282.9 |
| <i>Gross margin</i> | 83.7 | 84.5 | 85.4 | 86.2 | 87.1 | 87.9 | 88.8 | 89.7 | 90.6 | 91.5 | 92.4 | 93.4 | 94.3 |
| General expenses | 53.6 | 54.1 | 54.6 | 55.2 | 55.7 | 56.3 | 56.8 | 57.4 | 58.0 | 58.6 | 59.2 | 59.7 | 60.3 |
| Interests | 0.0 | 11.8 | 10.7 | 9.6 | 8.5 | 7.4 | 6.3 | 5.1 | 4.0 | 2.8 | 1.6 | 0.4 | 0.0 |
| <i>PBT</i> | 30.1 | 18.7 | 20.0 | 21.4 | 22.8 | 24.3 | 25.7 | 27.2 | 28.6 | 30.1 | 31.7 | 33.2 | 33.9 |
| Taxes (40%) | 12.0 | 7.5 | 8.0 | 8.6 | 9.1 | 9.7 | 10.3 | 10.9 | 11.5 | 12.1 | 12.7 | 13.3 | 13.6 |
| Net income | 18.1 | 11.2 | 12.0 | 12.9 | 13.7 | 14.6 | 15.4 | 16.3 | 17.2 | 18.1 | 19.0 | 19.9 | 20.4 |
| Dividends paid | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 162.8 | 0.0 |

| | | | | | | | | | | | | | |
|-------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-----|-----|-----|-------|
| Initial stock | 201 | 2,572 | 2,370 | 2,165 | 1,958 | 1,749 | 1,538 | 1,325 | 1,109 | 892 | 672 | 450 | 226 |
| + Purchases | 2,572 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 2,899 |
| + Labor and other | 50 | 51 | 51 | 52 | 52 | 53 | 53 | 54 | 54 | 55 | 55 | 56 | 57 |
| - cost of sales | 251 | 254 | 256 | 259 | 261 | 264 | 266 | 269 | 272 | 275 | 277 | 280 | 283 |
| Final stock | 2,572 | 2,370 | 2,165 | 1,958 | 1,749 | 1,538 | 1,325 | 1,109 | 892 | 672 | 450 | 226 | 2,899 |

Figure 2. Seasonality of monthly FCF



3. Valuation of Russoil Using Monthly Data

On November 2003, the monthly risk free rate was 0.4% and the monthly market risk premium was assumed to be 0.45%. The unlevered beta of the company was assumed to be 1.0. Then, the monthly unlevered cost of equity (K_u) was 0.85%.

Using the Adjusted present value (APV) formula, the valuation of the company at the end of November 2003 and at the end of December 2003 appears on table 3. The Value of tax shields is calculated according to Fernandez (2003).

Table 3. Valuation of Russoil using APV with monthly data

| | 11/03 | 12/03 |
|--------------------------|---------|---------|
| K_u | 0.85% | 0.85% |
| $V_u = PV(K_u; FCF)$ | 859.0 | 3,219.8 |
| $VTS = PV(K_u; D T K_u)$ | 307.0 | 309.6 |
| $E + D = VTS + V_u$ | 1,166.0 | 3,529.4 |
| $E = (E+D) - D$ | 1,166.0 | 1,175.9 |

Table 4 shows the valuation using the Equity cash flow method and the WACC method. Using those methods, the WACC and the required return to equity (K_e) change every month, as it is shown on Figure 3. Note that $K_e = WACC = K_u = 0.85\%$ in the months that there is no debt. K_e is higher (WACC is lower) when the debt is higher.

The valuation results of table 4 are equals to those of table 3. Note that the equity values calculated for November and December accomplish the following equilibrium relation:

$$E_t = E_{t-1} (1+K_{et}) - ECF_t \quad (1)$$

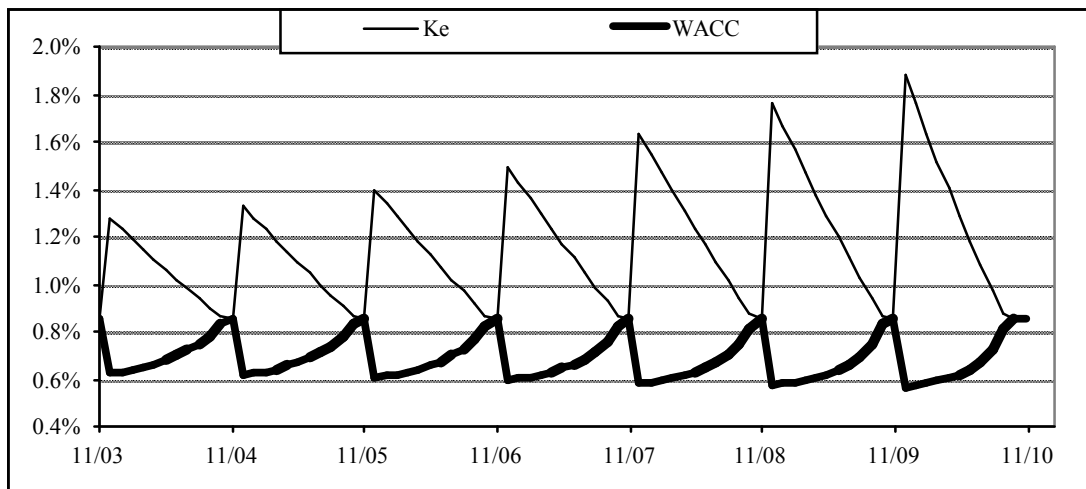
The values calculated for enterprise value ($EV = E + D$) accomplish the following equilibrium relation:

$$(Dt + Et) = (Dt - 1 + Et - 1) (1 + WACC_t) - FCF_t \quad (2)$$

Table 4. Valuation of Rusoil using the Equity cash flow method and the WACC method with monthly data

| | 11/03 | 12/03 |
|-------------------------|---------|---------|
| Ke | 0.85% | 1.27% |
| $E = PV(Ke; ECF)$ | 1,166.0 | 1,175.9 |
| WACC | 0.850% | 0.623% |
| $E + D = PV(WACC; FCF)$ | 1,166.0 | 3,529.4 |
| $E = (E + D) - D$ | 1,166.0 | 1,175.9 |

Figure 3. Seasonality of monthly Ke and WACC



4. Valuing the Company using Yearly Data

Table 5 shows the projected annual balance sheets and P&Ls of the company assuming that each year finishes in December. The balance sheets correspond to the monthly balance sheets of December. The P&Ls and the cash flows for every year are the sum of the 12 monthly P&Ls and cash flows from January to December.

Analogously, Table 6 shows the projected annual balance sheets and P&Ls of the company assuming that each year finishes in November (instead of in

December as Table 5). The balance sheets correspond to the monthly balance sheets of November. The P&Ls and the cash flows for every year are the sum of the 12 monthly P&Ls and cash flows from December to November next year.

Table 7 highlights the difference of the annual Free Cash Flows between tables 5 and 6, that is, depending upon we consider that every year finishes in December or in November. This difference has important consequences for valuation purposes. The annual equity cash flows are equal in tables 5 and 6.

**Table 5. Projected annual balance sheets, P&Ls and Cash flows of Russoil (\$000's)
in December of every year**

| | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
|---------------------|---------|---------|---------|---------|---------|----------|----------|----------|
| Cash | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 0.0 |
| Stocks | 2,572.4 | 2,898.6 | 3,266.2 | 3,680.5 | 4,147.2 | 4,378.0 | 4,013.1 | 0.0 |
| Fixed assets | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Total assets | 2,712.4 | 3,038.6 | 3,406.2 | 3,820.5 | 4,287.2 | 4,518.0 | 4,153.1 | 0.0 |
| Debt | 2,353.5 | 2,652.0 | 2,988.3 | 3,367.3 | 3,794.3 | 3,980.3 | 3,615.5 | 0.0 |
| Equity | 358.9 | 386.7 | 417.9 | 453.2 | 492.9 | 537.7 | 537.7 | 0.0 |
| Total | 2,712.4 | 3,038.6 | 3,406.2 | 3,820.5 | 4,287.2 | 4,518.0 | 4,153.1 | 0.0 |
| Sales | | 4,287.3 | 4,831.0 | 5,443.7 | 6,134.1 | 6,912.1 | 7,296.6 | 6,688.5 |
| Cost of sales | | 3,215.5 | 3,623.3 | 4,082.8 | 4,600.6 | 5,184.1 | 5,472.4 | 5,016.4 |
| <i>Gross margin</i> | | 1,071.8 | 1,207.8 | 1,360.9 | 1,533.5 | 1,728.0 | 1,824.1 | 1,672.1 |
| General expenses | | 686.0 | 773.0 | 871.0 | 981.5 | 1,105.9 | 1,167.5 | 1,070.2 |
| Depreciation | | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Interest | | 68.2 | 76.8 | 86.6 | 97.6 | 109.9 | 111.9 | 93.0 |
| <i>PBT</i> | | 317.7 | 358.0 | 403.4 | 454.5 | 512.2 | 544.8 | 508.9 |
| Taxes (40%) | | 127.1 | 143.2 | 161.3 | 181.8 | 204.9 | 217.9 | 203.6 |
| Net income | | 190.6 | 214.8 | 242.0 | 272.7 | 307.3 | 326.9 | 305.4 |
| Gross margin | | 1,071.8 | 1,207.8 | 1,360.9 | 1,533.5 | 1,728.0 | 1,824.1 | 1,672.1 |
| - general expenses | | -686.0 | -773.0 | -871.0 | -981.5 | -1,105.9 | -1,167.5 | -1,070.2 |
| NOPBT | | 385.9 | 434.8 | 489.9 | 552.1 | 622.1 | 656.7 | 602.0 |
| taxes on NOPBT | | -154.3 | -173.9 | -196.0 | -220.8 | -248.8 | -262.7 | -240.8 |
| NOPAT | | 231.5 | 260.9 | 294.0 | 331.2 | 373.3 | 394.0 | 361.2 |
| increase of WCR | | -326.2 | -367.6 | -414.2 | -466.8 | -230.7 | 364.8 | 4,153.1 |
| FCF | | -94.7 | -106.7 | -120.3 | -135.5 | 142.5 | 758.8 | 4,514.3 |
| + ΔD | | 298.5 | 336.3 | 379.0 | 427.1 | 186.0 | -364.8 | -3,615.5 |
| - int (1-T) | | -40.9 | -46.1 | -51.9 | -58.5 | -66.0 | -67.1 | -55.8 |
| ECF | | 162.8 | 183.5 | 206.8 | 233.0 | 262.5 | 326.9 | 843.0 |
| CFd | | -230.3 | -259.5 | -292.4 | -329.5 | -76.0 | 476.7 | 3,708.5 |

Table 6. Projected annual balance sheets, P&Ls and Cash flows of Russoil (\$000's) in November of every year

| | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
|---------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|
| Cash | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 140.0 | 0.0 |
| Stocks | 200.8 | 226.3 | 255.0 | 287.3 | 323.8 | 364.8 | 364.8 | 0.0 |
| Fixed assets | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Total assets | 340.8 | 366.3 | 395.0 | 427.3 | 463.8 | 504.8 | 504.8 | 0.0 |
| Accounts payable | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Debt | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| Equity | 340.8 | 366.3 | 395.0 | 427.3 | 463.8 | 504.8 | 504.8 | 0.0 |
| Total | 340.8 | 366.3 | 395.0 | 427.3 | 463.8 | 504.8 | 504.8 | 0.0 |
| Sales | 4,244.8 | 4,783.2 | 5,389.8 | 6,073.4 | 6,843.6 | 7,296.6 | 7,296.6 | |
| Cost of sales | 3,183.6 | 3,587.4 | 4,042.4 | 4,555.0 | 5,132.7 | 5,472.4 | 5,472.4 | |
| Gross margin | 1,061.2 | 1,195.8 | 1,347.5 | 1,518.3 | 1,710.9 | 1,824.1 | 1,824.1 | |
| General expenses | 679.2 | 765.3 | 862.4 | 971.7 | 1,095.0 | 1,167.5 | 1,167.5 | |
| Interest | 68.2 | 76.8 | 86.6 | 97.6 | 109.9 | 111.9 | 93.0 | |
| PBT | 313.9 | 353.7 | 398.5 | 449.1 | 506.0 | 544.8 | 563.7 | |
| Taxes (40%) | 125.5 | 141.5 | 159.4 | 179.6 | 202.4 | 217.9 | 225.5 | |
| Net income | 188.3 | 212.2 | 239.1 | 269.4 | 303.6 | 326.9 | 338.2 | |
| Gross margin | 1,061.2 | 1,195.8 | 1,347.5 | 1,518.3 | 1,710.9 | 1,824.1 | 1,824.1 | |
| - general expenses | -679.2 | -765.3 | -862.4 | -971.7 | -1,095.0 | -1,167.5 | -1,167.5 | |
| NOPBT | 382.0 | 430.5 | 485.1 | 546.6 | 615.9 | 656.7 | 656.7 | |
| taxes on NOPBT | -152.8 | -172.2 | -194.0 | -218.6 | -246.4 | -262.7 | -262.7 | |
| NOPAT | 229.2 | 258.3 | 291.1 | 328.0 | 369.6 | 394.0 | 394.0 | |
| - increase of WCR | -25.5 | -28.7 | -32.3 | -36.4 | -41.1 | 0.0 | 504.8 | |
| FCF | 203.8 | 229.6 | 258.7 | 291.5 | 328.5 | 394.0 | 898.8 | |
| + ΔD | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | |
| - int (1-T) | -40.9 | -46.1 | -51.9 | -58.5 | -66.0 | -67.1 | -55.8 | |
| ECF | 162.8 | 183.5 | 206.8 | 233.0 | 262.5 | 326.9 | 843.0 | |

Table 7. Annual Free Cash Flows of Russoil (\$000's) from tables 5 and 6, that is, depending upon we consider that every year finishes in December or in November.

| | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
|-----------------------|------|------|------|------|------|------|-------|
| FCF - November | 204 | 230 | 259 | 292 | 328 | 394 | 899 |
| FCF - December | -95 | -107 | -120 | -136 | 143 | 759 | 4,514 |

If we value Russoil using the APV method and the annual data of tables 5 and 6, we get very different values to the ones obtained on table 3. The annual required return to the unlevered equity (K_{ua}) should be: $K_{ua} = (1+K_u)^{12} - 1 = (1+0.0085)^{12} - 1 = 10.6906\%$. Table 8 contains the valuation of Russoil using the annual FCFs of tables 5 and 6, without taking into consideration the seasonality. Column 1 contains the unlevered equity value, column 2 the value of tax shields,

column 3 the enterprise value, column 4 the debt at the beginning of the year and column 5 the equity value obtained using annual data. Column 6 has the Equity value obtained using monthly data (the correct value), and column 7 the error of using annual data without adjustments. It may be seen that the Enterprise Value (EV = E+D) in November is 1609.8 (instead of 1166 in table 3) and in December is 3,003.7 (instead of 3529.4 in table 3). The equity value (E) in November is 1609.8 (instead of 1166 in table 3) and in December is 650.2 (instead of 1175.9 in table 3). The value of the unlevered equity (Vu) in November is 1609.8 (instead of 859 in table 3), and in December is 2363.9 (instead of 3219.8 in table 3).

Obviously, the right values are those of table 3. **Columns 1, 2, 3 and 5 of table 8** are wrong because we did not take into consideration the seasonality.

Table 8. Valuation of Russoil using annual data, without taking into consideration the seasonality

| Error = (E annual data - E monthly data) / E monthly data | | | | | | | |
|--|---------|-------|---------|---------|---------------|----------------|--------|
| Column # | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| | Vu | VTS | D+E | -D | E annual data | E monthly data | Error |
| 11/03 | 1,609.8 | 0.0 | 1,609.8 | 0.0 | 1,609.8 | 1,166.0 | 38.1% |
| 12/03 | 2,363.9 | 639.7 | 3,003.7 | 2,353.5 | 650.2 | 1,175.9 | -44.7% |
| 1/04 | 2,297.5 | 579.8 | 2,877.3 | 2,139.5 | 737.8 | 1,190.8 | -38.0% |
| 2/04 | 2,230.0 | 519.2 | 2,749.2 | 1,922.6 | 826.6 | 1,205.4 | -31.4% |
| 3/04 | 2,161.4 | 458.0 | 2,619.4 | 1,702.8 | 916.6 | 1,219.7 | -24.9% |
| 4/04 | 2,091.6 | 396.2 | 2,487.8 | 1,480.1 | 1,007.6 | 1,233.7 | -18.3% |
| 5/04 | 2,020.7 | 333.7 | 2,354.4 | 1,254.5 | 1,099.9 | 1,247.3 | -11.8% |
| 6/04 | 1,948.7 | 270.6 | 2,219.2 | 1,025.9 | 1,193.3 | 1,260.5 | -5.3% |
| 7/04 | 1,875.4 | 206.8 | 2,082.3 | 794.3 | 1,287.9 | 1,273.4 | 1.1% |
| 8/04 | 1,801.1 | 142.4 | 1,943.4 | 559.7 | 1,383.8 | 1,285.9 | 7.6% |
| 9/04 | 1,725.5 | 77.3 | 1,802.8 | 322.0 | 1,480.8 | 1,298.0 | 14.1% |
| 10/04 | 1,648.7 | 17.9 | 1,666.6 | 81.1 | 1,585.5 | 1,309.7 | 21.1% |
| 11/04 | 1,594.3 | 0.0 | 1,594.3 | 0.0 | 1,594.3 | 1,158.1 | 37.7% |

Tables 9 and 10 provide us with the sensitivity of the error of using annual data, without taking into consideration the seasonality, with respect to the growth rate and the discount rate. It may be seen that the error is higher with higher growth and higher discount rates.

Table 9. Sensitivity of the error of valuing Russoil using annual data, without taking into consideration the seasonality, with respect to the growth rate

| | | g | | | | | |
|----------|----------------|--------|--------|--------|--------|--------|--------|
| | | 0.0% | 0.5% | 1.0% | 1.5% | 2.0% | 2.5% |
| November | E monthly data | 813.2 | 966.9 | 1166.0 | 1425.9 | 1767.6 | 2219.7 |
| November | E annual data | 1082.5 | 1311.3 | 1609.8 | 2001.6 | 2519.3 | 3206.8 |
| | error | 33.1% | 35.6% | 38.1% | 40.4% | 42.5% | 44.5% |
| December | E monthly data | 820.1 | 975.1 | 1175.9 | 1438.0 | 1782.7 | 2238.5 |
| December | E annual data | 488.6 | 559.6 | 650.2 | 767.0 | 918.9 | 1118.2 |
| | error | -40.4% | -42.6% | -44.7% | -46.7% | -48.5% | -50.0% |

Table 10. Sensitivity of the error of valuing Russoil using annual data, without taking into consideration the seasonality, with respect to the discount rate

| | | βu | | | | | | | |
|----------|----------------|---------|---------|---------|---------|---------|---------|---------|---------|
| | | 0.25 | 0.50 | 0.75 | 1.00 | 1.50 | 2.00 | 2.50 | 3.00 |
| November | E monthly data | 1,631.2 | 1,463.0 | 1,308.3 | 1,166.0 | 914.1 | 700.3 | 518.3 | 363.2 |
| November | E annual data | 1,937.5 | 1,819.9 | 1,710.9 | 1,609.8 | 1,428.9 | 1,272.8 | 1,137.7 | 1,020.5 |
| | error | 18.8% | 24.4% | 30.8% | 38.1% | 56.3% | 81.8% | 119.5% | 181.0% |
| December | E monthly data | 1,639.5 | 1,472.2 | 1,318.0 | 1,175.9 | 924.0 | 709.4 | 526.2 | 369.5 |
| December | E annual data | 1,270.2 | 1,044.5 | 838.4 | 650.2 | 321.2 | 46.6 | -182.9 | -374.8 |
| | error | -22.5% | -29.1% | -36.4% | -44.7% | -65.2% | -93.4% | -134.8% | -201.4% |

There is the issue of within-year compounding of the free cash flows, but it explains only a minor part of the error, as we will see on next section.

4.1. Adjustments needed for valuing the company using yearly data

When dealing with seasonality, it is important to isolate it. One way of doing it is to decompose the Free cash flow in two parts: the free cash flow without purchases of seeds (FCF. purchases =0), and the seeds purchases² (Purchases).

Figures 4 and 5 show the evolution of both magnitudes. The free cash flow without changes in Working Capital Requirements (FCF. purchases =0) grows at a monthly rate of 1% until December 2008, and since then until October 2010 remains constant. In November 2010, The free cash flow without changes in Working Capital Requirements (FCF. purchases =0) is 140 higher than in October due to the recovery of the cash.

² What really matters is the payment of the seeds. In the case of Russoil, as payments are done in cash, the purchase and the payment of seeds happens in the same moment.

Figure 4. Russoil. Monthly free cash flow without Purchases of raw materials (FCF. purchases=0)

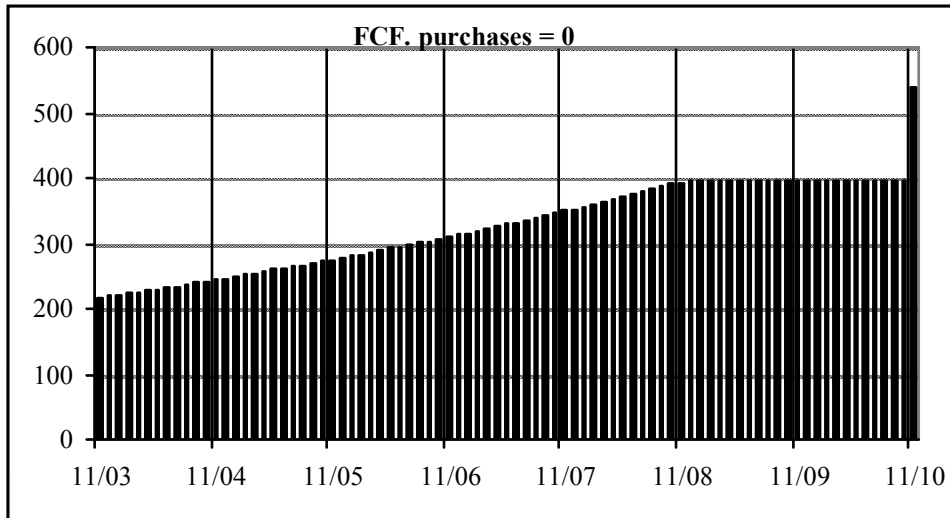
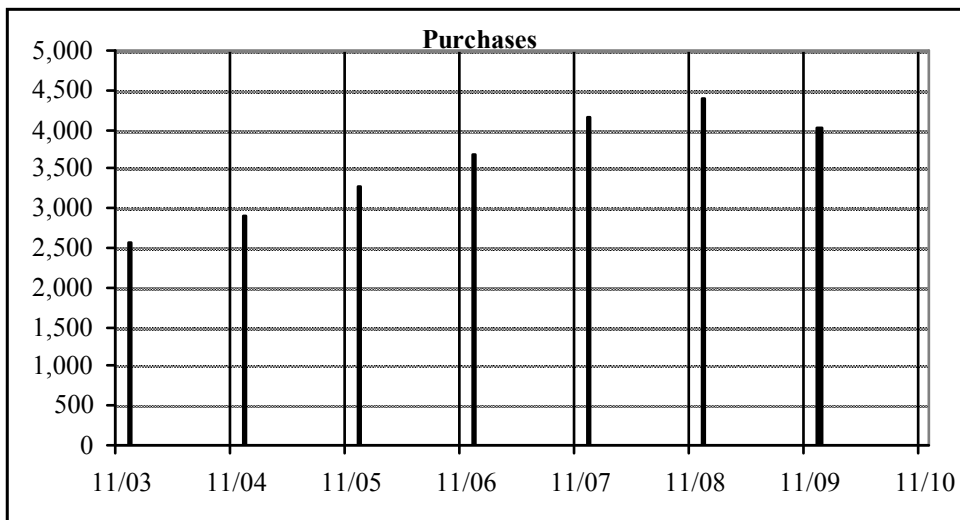


Figure 5. Russoil. Monthly Purchases (and payments) of seeds



The seasonality of Russoil is clearly due to the Purchases.

The value of the unlevered equity (V_u) may be decomposed in the sum of the present values of the two components of the free cash flows (PV_m means present value with monthly data)

$$V_u = PV_m(\text{FCF}; K_u) = PV_m(\text{FCF. purchases}=0; K_u) - PV_m(\text{Purchases}; K_u) \quad (3)$$

Table 11 contains the present value of the monthly free cash flows of the different years.

Table 11. Valuation of Russoil using monthly data.

| Value in November 2003 | | Present value of monthly free cash flows | | |
|-------------------------------|-----------------|--|--------------------|-----------|
| | | FCF | FCF. purchases = 0 | Purchases |
| December 2003 | - November 2004 | 75.3 | 2,626.0 | 2,550.7 |
| December 2004 | - November 2005 | 76.7 | 2,673.3 | 2,596.6 |
| December 2005 | - November 2006 | 78.0 | 2,721.4 | 2,643.3 |
| December 2006 | - November 2007 | 79.5 | 2,770.3 | 2,690.9 |
| December 2007 | - November 2008 | 80.9 | 2,820.2 | 2,739.3 |
| December 2008 | - November 2009 | 106.8 | 2,719.2 | 2,612.4 |
| December 2009 | - November 2010 | 361.9 | 2,525.3 | 2,163.4 |
| SUM | | 859.0 | 18,855.6 | 17,996.6 |

| Value in December 2003 | | Value in December 2003 | | |
|-------------------------------|-----------------|--|--------------------|-----------|
| | | Present value of monthly free cash flows | | |
| | | FCF | FCF. purchases = 0 | Purchases |
| January 2004 | - December 2004 | 33.6 | 2,652.3 | 2,618.7 |
| January 2005 | - December 2005 | 34.2 | 2,700.0 | 2,665.8 |
| January 2006 | - December 2006 | 34.8 | 2,748.6 | 2,713.8 |
| January 2007 | - December 2007 | 35.4 | 2,798.0 | 2,762.6 |
| January 2008 | - December 2008 | 213.8 | 2,848.4 | 2,634.6 |
| January 2009 | - December 2009 | 537.4 | 2,719.2 | 2,181.8 |
| January 2010 | - December 2010 | 2,330.6 | 2,330.6 | 0.0 |
| SUM | | 3,219.8 | 18,797.0 | 15,577.2 |

Using annual data, the value of the unlevered equity (V_u) may be decomposed in the sum of the present values of the two components of the free cash flows (PVA means present value with annual data)

$$V_u = PVA(\text{FCF. purchases} = 0; K_{uae}) - PVA(\text{Purchases}; K_{uas}) \quad (4)$$

In a correct valuation, (3) must equal (4).

To calculate the PVA (FCF. purchases = 0; K_{uae}) using annual data, it is worth to take a look at Appendix 1. In Appendix 1, we calculate the annual discount rate (K_{uae} needed to discount annual free cash flows) such that the present value of the monthly free cash flows (that grow at a monthly rate g) equals the present value of the annual free cash flow.

To calculate the PVA (Purchases; K_{uas}) using annual data, it is worth to take a look at Appendix 2. In Appendix 2, we calculate the annual discount rate (K_{uas} needed to discount annual purchases) that ensures that the present value of the monthly purchases (one cash flow per year) equals the present value of the annual purchases.

Table 12 contains the present value of the annual free cash flows taking into consideration the adjustments of appendixes 1 and 2. Lines 1 to 12 contain the valuation in November 2003, and Lines 13 to 24 contain the valuation in December 2003. Lines 1 and 7 contain the free cash flow decomposition. Line 2 contains the monthly growth of the monthly free cash flows (g). Line 3 is the calculation of the rate Kuae according to the formulas of Appendix 1. Line 4 contains the rate at which should be discounted the cash flows of line 1. Line 5 is the inverse of line 4. Line 6 is the first present value of equation (4): PVa (FCF. purchases =0; Kuae). Line 8 contains the month (after the valuation date) in which the purchase and payment of the raw materials takes place (n). Line 9 is the calculation of the rate Kuas according to the formula of Appendix 2. Line 10 contains the rate at which should be discounted the cash flows of line 7. Line 11 is the inverse of line 10. Line 12 is the second present value of equation (4): PVa (Purchases;Kuas).

Table 12. Valuation of Russoil using annual data, taking into consideration the seasonality through the discount rates

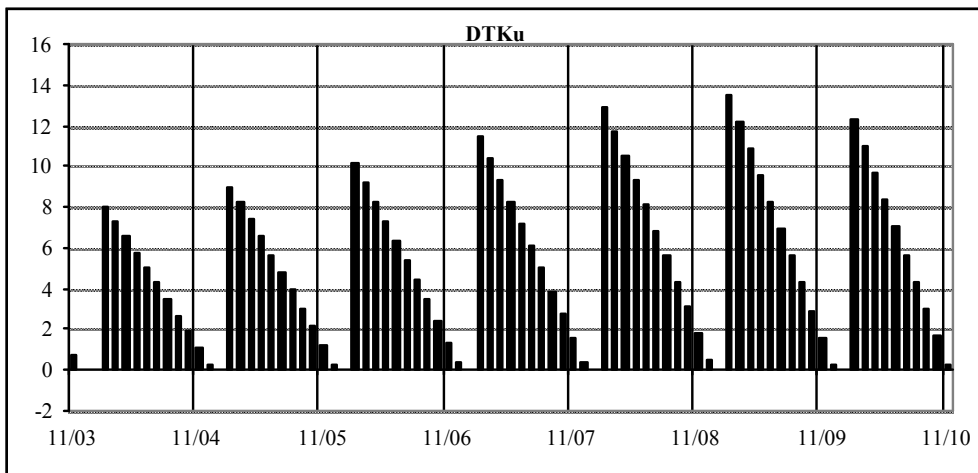
| line | NOVEMBER | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | Sum | |
|------|---------------------------|-------------|-------------|-------------|-------------|-------------|-------------|----------------|------------|--|
| 1 | FCF. purchases = 0 | 2,776.1 | 3,128.2 | 3,524.9 | 3,972.0 | 4,475.7 | 4,772.0 | 4,912.0 | 27,561.0 | |
| 2 | g | 1.0% | 1.0% | 1.0% | 1.0% | 1.0% | 0.0% | 0.00% | | |
| 3 | Kuae | 5.72% | 5.72% | 5.72% | 5.72% | 5.72% | 5.61% | 5.61% | | |
| 4 | $(1+Kuae)(1+Kua)^{n-1}$ | 1.0572 | 1.1702 | 1.2953 | 1.4338 | 1.5870 | 1.7549 | 1.9426 | | |
| 5 | Discount factor | 0.9459 | 0.8546 | 0.7720 | 0.6975 | 0.6301 | 0.5698 | 0.5148 | | |
| 6 | PV(FCF. purchases = 0) | 2,626.0 | 2,673.3 | 2,721.4 | 2,770.3 | 2,820.2 | 2,719.2 | 2,528.6 | 18,858.9 | |
| 7 | Purchases | 2,572.4 | 2,898.6 | 3,266.2 | 3,680.5 | 4,147.2 | 4,378.0 | 4,013.1 | 24,956.0 | |
| 8 | n | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | |
| 9 | Kuas | 0.85% | 0.85% | 0.85% | 0.85% | 0.85% | 0.85% | 0.85% | | |
| 10 | $(1+Kuas)(1+Kua)^{n-1}$ | 1.0085 | 1.1163 | 1.2357 | 1.3678 | 1.5140 | 1.6758 | 1.8550 | | |
| 11 | Discount factor | 0.9916 | 0.8958 | 0.8093 | 0.7311 | 0.6605 | 0.5967 | 0.5391 | | |
| 12 | PV(Purchases) | 2,550.7 | 2,596.6 | 2,643.3 | 2,690.9 | 2,739.3 | 2,612.4 | 2,163.4 | 17,996.6 | |
| | DECEMBER | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | Sum | |
| 13 | FCF. purchases = 0 | 2,803.9 | 3,159.5 | 3,560.2 | 4,011.7 | 4,520.5 | 4,772.0 | 4,514.3 | 27,342.1 | |
| 14 | g | 1.0% | 1.0% | 1.0% | 1.0% | 1.0% | 0.0% | 0.0% | | |
| 15 | Kuae | 5.72% | 5.72% | 5.72% | 5.72% | 5.72% | 5.61% | 5.17%* | | |
| 16 | $(1+Kuae)(1+Kua)^{n-1}$ | 1.0572 | 1.1702 | 1.2953 | 1.4338 | 1.5870 | 1.7549 | 1.9345 | | |
| 17 | Discount factor | 0.9459 | 0.8546 | 0.7720 | 0.6975 | 0.6301 | 0.5698 | 0.5169 | | |
| 18 | PV(FCF. purchases = 0) | 2,652.3 | 2,700.0 | 2,748.6 | 2,798.0 | 2,848.4 | 2,719.2 | 2,333.6 | 18,800.0 | |
| | * 11 months in 2010 | | | | | | | | | |
| 19 | Purchases | 2,898.6 | 3,266.2 | 3,680.5 | 4,147.2 | 4,378.0 | 4,013.1 | 0.0 | 22,383.6 | |
| 20 | n | 12 | 12 | 12 | 12 | 12 | 12 | 12 | | |
| 21 | Kuas | 10.69% | 10.69% | 10.69% | 10.69% | 10.69% | 10.69% | 10.69% | | |
| 22 | $(1+Kuas)(1+Kua)^{n-1}$ | 1.1069 | 1.2252 | 1.3562 | 1.5012 | 1.6617 | 1.8394 | 2.0360 | | |
| 23 | Discount factor | 0.9034 | 0.8162 | 0.7373 | 0.6661 | 0.6018 | 0.5437 | 0.4912 | | |
| 24 | PV(Purchases) | 2,618.7 | 2,665.8 | 2,713.8 | 2,762.6 | 2,634.6 | 2,181.8 | 0.0 | 15,577.2 | |

Comparing tables 11 and 12, it may be seen that all present values match except the PVa (FCF. purchases = 0) in year 2010 (lines 6 and 18 of table 12). Why? Because, as it may be seen on figures 2 and 4, the Free Cash Flow of November 2010 is \$140,000 bigger than the Free Cash Flow of October 2010 because on November 2010 the Free Cash Flow incorporates the Cash that the company had. Correcting the effect of these \$140,000, the results of table 11 and 12 match³.

3.2. Calculating the Value of tax shields using annual data

We show in figure 2 that Debt is very seasonal. The Value of tax shields is the present value of (D T Ku) discounted at Ku. D T Ku is also very seasonal as may be seen in figure 6.

Figure 6. Russoil. Seasonality of monthly D T Ku



As debt (D) is a balance sheet measure, it is very complex to model it. Table 13 has the discount factors (column 5) and the annual discount rates (column 6) that ensure that the Value of tax shields calculated using monthly data equals the Value of tax shields calculated using annual data.

³ **November.** The PV (FCF. purchases = 0, in year 2010) is 2,525.3 in table 11 (the correct one) and 2,528.6 in table 12 (line 6). The present value of these \$140,000 is calculated in table 12 using a discount factor of 0.5148 (1/1.9426). But these 140 are a monthly cash flow in the 12th month, as the ones valued in Appendix 2. The appropriate Kuas rate (for Ku = 0.85%; n = 12) is 10.6906227%. In this case, $(1+Kuas)(1+Kua)^{n-1} = (1+10.690623\%)(1+10.690623\%)^6 = 2.03599$. Then, in table 12 we must add $-3.307 = 140 / 2.03599 - 140 / 1.9426$. Note that $2,528.6 - 3.307 = 2,525.3$. **For December,** the appropriate Kuas rate is (for Ku = 0.85%; n = 11) 9.7577%. In this case, $(1+Kuas)(1+Kua)^{n-1} = (1+9.7577\%)(1+10.690623\%)^6 = 2.01883$. Then, in table 10 we must add $3.023 = 140 / 2.01883 - 140 / 1.9345$. Note that $2,333.6 - 3.023 = 2,330.6$.

An easier approach and a good approximation, is to consider the average debt when using annual data⁴. The error of this approximation is very small, as we show in table 14. Column 1 contains the correct value (the Value of tax shields calculated using monthly data), column 5 contains the approximation (the Value of tax shields calculated using annual data), and column 6 contains the error of the approximation. The errors are small. Tables 15 and 16 contain sensitivity analysis of the errors and confirm that the errors of this approximation are small. The error grows with the discount rate.

Table 17 shows that the error of this approximation for the VTS of Russoil ranges between -2% and 2.2%. Then, to consider the average debt when using annual data is a very good approximation for calculating the Value of Tax Shields. However, we will see in next section that to consider the average debt and average Working Capital requirements when using annual data is a worse approximation for calculating the Value of the unlevered company and the equity value.

Table 13. Correct Discount factor and correct annual discount rate to calculate the value of tax shields using annual data

| | PV (DTKu;Ku) monthly | Da T Kua | Average annual debt (Da) | 1/ discount | Discount factor | Annual discount rate |
|------------------------------------|----------------------------|-------------|-----------------------------|----------------|--------------------|-------------------------|
| Column # | 1 | 2 | 3 | 4 | 5 | 6 |
| December - November 2003 - 2004 | 44.4 | 48.6 | 1,136.3 | 1.0947 | 0.9135 | 9.47% |
| December - November 2004 - 2005 | 45.2 | 54.8 | 1,280.5 | 1.2117 | 0.8253 | 10.69% |
| December - November 2005 - 2006 | 46.0 | 61.7 | 1,442.8 | 1.3413 | 0.7456 | 10.69% |
| December - November 2006 - 2007 | 46.8 | 69.5 | 1,625.8 | 1.4847 | 0.6736 | 10.69% |
| December - November 2007 - 2008 | 47.7 | 78.3 | 1,832.0 | 1.6434 | 0.6085 | 10.69% |
| December - November 2008 - 2009 | 43.9 | 79.7 | 1,864.7 | 1.8177 | 0.5501 | 10.61% |
| December - November 2009 - 2010 | 33.0 | 66.3 | 1,550.7 | 2.0068 | 0.4983 | 10.40% |

⁴ But to calculate the average debt, we need to forecast the monthly balance sheets.

Table 14. Error due to calculate the value of tax shields using annual data and average debt

| | PV (DTKu;Ku) monthly | Da (average debt) | Kua | factor | PV (DaTKua;Kua) annual | error |
|-------------------------------|----------------------------|-------------------------|--------|--------|------------------------------|-------|
| Column # | 1 | 2 | 3 | 4 | 5 | 6 |
| December 2003 - November 2004 | 44.4 | 1,136.3 | 10.69% | 1.1069 | 43.9 | -1.1% |
| December 2004 - November 2005 | 45.2 | 1,280.5 | 10.69% | 1.2252 | 44.7 | -1.1% |
| December 2005 - November 2006 | 46.0 | 1,442.8 | 10.69% | 1.3562 | 45.5 | -1.1% |
| December 2006 - November 2007 | 46.8 | 1,625.8 | 10.69% | 1.5012 | 46.3 | -1.1% |
| December 2007 - November 2008 | 47.7 | 1,832.0 | 10.69% | 1.6617 | 47.1 | -1.1% |
| December 2008 - November 2009 | 43.9 | 1,864.7 | 10.69% | 1.8394 | 43.4 | -1.2% |
| December 2009 - November 2010 | 33.0 | 1,550.7 | 10.69% | 2.0360 | 32.6 | -1.4% |
| SUM | 307.0 | | | | 303.5 | -1.1% |

| | PV (DTKu;Ku) monthly | Da (average debt) | Kua | factor | PV (DaTKua;Kua) annual | error |
|------------------------------|----------------------------|-------------------------|--------|--------|------------------------------|-------|
| January 2004 - December 2004 | 44.8 | 1,136.3 | 10.69% | 1.1069 | 43.9 | -1.9% |
| January 2005 - December 2005 | 45.6 | 1,280.5 | 10.69% | 1.2252 | 44.7 | -1.9% |
| January 2006 - December 2006 | 46.4 | 1,442.8 | 10.69% | 1.3562 | 45.5 | -1.9% |
| January 2007 - December 2007 | 47.2 | 1,625.8 | 10.69% | 1.5012 | 46.3 | -1.9% |
| January 2008 - December 2008 | 48.1 | 1,832.0 | 10.69% | 1.6617 | 47.1 | -1.9% |
| January 2009 - December 2009 | 44.2 | 1,864.7 | 10.69% | 1.8394 | 43.4 | -2.0% |
| January 2010 - December 2010 | 33.3 | 1,550.7 | 10.69% | 2.0360 | 32.6 | -2.3% |
| SUM | 309.6 | | | | 303.5 | -2.0% |

Table 15. Sensitivity to the monthly growth rate of the error due to calculate the value of tax shields using annual data and average debt

| | g | | | | | |
|------------------------|-------|-------|-------|-------|-------|-------|
| | 0.0% | 0.5% | 1.0% | 1.5% | 2.0% | 2.5% |
| Error in December 2010 | -2.0% | -2.0% | -2.0% | -2.0% | -1.9% | -1.9% |
| Error in November 2010 | -1.2% | -1.2% | -1.1% | -1.1% | -1.1% | -1.1% |

Table 16. Sensitivity to the discount rate of the error due to calculate the value of tax shields using annual data and average debt

| | β_u | | | | | | | |
|------------------------|-----------|-------|-------|-------|-------|-------|-------|-------|
| | 0.25 | 0.50 | 0.75 | 1.00 | 1.50 | 2.00 | 2.50 | 3.00 |
| Error in December 2010 | -1.2% | -1.5% | -1.7% | -2.0% | -2.5% | -3.0% | -3.5% | -4.0% |
| Error in November 2010 | -0.7% | -0.9% | -1.0% | -1.1% | -1.4% | -1.7% | -2.0% | -2.3% |

Table 17. Error due to calculate the value of tax shields of Russoil using annual data and average debt, instead of monthly data

| | VTS calculated with annual data, and average debt | VTS calculated with monthly data | Error of using annual data |
|-------|---|----------------------------------|----------------------------|
| 11/03 | 303.5 | 307.0 | -1.1% |
| 12/03 | 303.5 | 309.6 | -2.0% |
| 1/04 | 300.8 | 304.2 | -1.1% |
| 2/04 | 300.2 | 299.5 | 0.2% |
| 3/04 | 299.2 | 295.5 | 1.2% |
| 4/04 | 297.9 | 292.3 | 1.9% |
| 5/04 | 296.2 | 289.7 | 2.2% |
| 6/04 | 294.3 | 287.9 | 2.2% |
| 7/04 | 292.2 | 286.9 | 1.8% |
| 8/04 | 290.0 | 286.6 | 1.2% |
| 9/04 | 288.2 | 287.1 | 0.4% |
| 10/04 | 287.4 | 288.5 | -0.4% |
| 11/04 | 287.3 | 290.7 | -1.2% |

5. Error due to value a seasonal company using annual data and average debt and average working capital requirements, instead of monthly data

Some professors argue that the valuation of a seasonal company may be computed using annual data, as long as we use average debt and average working capital requirements. This is a bad approximation as it is shown in tables 18 and 19.

Table 18 provides the valuation of Russoil in December 2003, using annual data, average debt and average working capital requirements. Line 2 contains the average working capital requirements and line 4 the average debt. Lines 5 to 11 are the calculation of the annual free cash flow using the the average working capital requirements calculated in line 2. Line 12 contains the present value of the free cash flows of line 11. Line 13 is the Value of Tax Shields using the average debt calculated on line 4. Line 15 is the Equity value using the APV equation:

$$E = Vu + VTS - Da \quad (5)$$

Note that using averages, only E (line 15) and VTS (line 13) are approximations of the true values. The value of Vu calculated is not an approximation of the true Vu.

Table 18. Valuation of Russoil using annual data, average debt and average working capital requirements. Valuation performed in December 2003.

| Line | | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 |
|------|--------------------------------------|---------|---------|---------|---------|---------|----------|----------|----------|
| 1 | Stocks | 2,572.4 | 2,898.6 | 3,266.2 | 3,680.5 | 4,147.2 | 4,378.0 | 4,013.1 | 0.0 |
| 2 | Stocks average | 1,418.8 | 1,598.7 | 1,801.5 | 2,029.9 | 2,287.4 | 2,371.4 | 2,006.6 | 0.0 |
| 3 | Debt | 2,353.5 | 2,652.0 | 2,988.3 | 3,367.3 | 3,794.3 | 3,980.3 | 3,615.5 | 0.0 |
| 4 | Da (average debt) | 1,136.3 | 1,280.5 | 1,442.8 | 1,625.8 | 1,832.0 | 1,864.7 | 1,550.7 | |
| 5 | Gross margin | | 1,071.8 | 1,207.8 | 1,360.9 | 1,533.5 | 1,728.0 | 1,824.1 | 1,672.1 |
| 6 | - general expenses | | -686.0 | -773.0 | -871.0 | -981.5 | -1,105.9 | -1,167.5 | -1,070.2 |
| 7 | NOPBT | | 385.9 | 434.8 | 489.9 | 552.1 | 622.1 | 656.7 | 602.0 |
| 8 | taxes on NOPBT | | -154.3 | -173.9 | -196.0 | -220.8 | -248.8 | -262.7 | -240.8 |
| 9 | NOPAT | | 231.5 | 260.9 | 294.0 | 331.2 | 373.3 | 394.0 | 361.2 |
| 10 | - increase of WCR average | | -179.9 | -202.8 | -228.5 | -257.4 | -84.0 | 364.8 | 2,146.6 |
| 11 | FCFav (using WCR average) | | 51.6 | 58.1 | 65.5 | 73.8 | 289.3 | 758.8 | 2,507.7 |
| 12 | $V_u = PV(FCFav; K_{ua})$ | 2,009.8 | 2,173.1 | 2,347.3 | 2,532.7 | 2,729.7 | 2,732.3 | 2,265.5 | |
| 13 | $VTS = PV(Dav \ T \ K_{ua}; K_{ua})$ | 303.5 | 287.3 | 263.3 | 229.7 | 184.7 | 126.2 | 59.9 | |
| 14 | $EV = V_u + VTS$ | 2,313.3 | 2,460.4 | 2,610.6 | 2,762.5 | 2,914.5 | 2,858.4 | 2,325.4 | |
| 15 | $E = EV - Da$ | 1,179.7 | 1,185.0 | 1,175.6 | 1,147.9 | 1,097.8 | 1,017.9 | 831.9 | |

Table 19 is a comparison of the equity values obtained using annual data, average debt and average working capital requirements, with the true equity value (using monthly data). The error of adjusting only by using average debt and average working capital requirements ranges from -17.9% to 8.5%.

Table 19. Equity value using annual data, average debt and average working capital requirements. Comparison with the equity value using monthly data

| | Equity value calculated with annual data and average values $E = V_u + VTS - Da$ | E monthly | Error |
|-------|---|-----------|--------|
| 11/03 | 1,179.7 | 1,166.0 | 1.2% |
| 12/03 | 1,176.9 | 1,175.9 | 0.1% |
| 1/04 | 1,178.4 | 1,190.8 | -1.0% |
| 2/04 | 1,174.9 | 1,205.4 | -2.5% |
| 3/04 | 1,172.0 | 1,219.7 | -3.9% |
| 4/04 | 1,169.9 | 1,233.7 | -5.2% |
| 5/04 | 1,168.4 | 1,247.3 | -6.3% |
| 6/04 | 1,167.7 | 1,260.5 | -7.4% |
| 7/04 | 1,167.7 | 1,273.4 | -8.3% |
| 8/04 | 1,168.6 | 1,285.9 | -9.1% |
| 9/04 | 1,170.6 | 1,298.0 | -9.8% |
| 10/04 | 1,174.1 | 1,309.7 | -10.4% |
| 11/04 | 1,185.0 | 1,158.1 | 2.3% |

| (Cont'd) | Equity value calculated with annual data and average values $E = V_u + VTS - Da$ | E monthly | Error |
|----------|--|-----------|--------|
| 12/04 | 1,180.0 | 1,168.0 | 1.0% |
| 1/05 | 1,181.1 | 1,183.5 | -0.2% |
| 2/05 | 1,176.7 | 1,198.6 | -1.8% |
| 3/05 | 1,172.8 | 1,213.3 | -3.3% |
| 4/05 | 1,169.5 | 1,227.7 | -4.7% |
| 5/05 | 1,166.8 | 1,241.6 | -6.0% |
| 6/05 | 1,164.8 | 1,255.1 | -7.2% |
| 7/05 | 1,163.5 | 1,268.2 | -8.3% |
| 8/05 | 1,163.0 | 1,280.9 | -9.2% |
| 9/05 | 1,163.5 | 1,293.1 | -10.0% |
| 10/05 | 1,165.5 | 1,304.9 | -10.7% |
| 11/05 | 1,175.6 | 1,132.6 | 3.8% |
| 12/05 | 1,167.7 | 1,142.3 | 2.2% |
| 11/07 | 1,097.8 | 1,012.0 | 8.5% |
| 12/07 | 1,082.4 | 1,020.6 | 6.1% |
| 1/09 | 987.4 | 930.4 | 6.1% |
| 2/09 | 971.8 | 945.8 | 2.7% |
| 3/09 | 956.4 | 960.6 | -0.4% |
| 4/09 | 941.2 | 974.7 | -3.4% |
| 5/09 | 926.1 | 988.1 | -6.3% |
| 6/09 | 911.3 | 1,000.8 | -8.9% |
| 7/09 | 896.8 | 1,012.7 | -11.5% |
| 8/09 | 882.7 | 1,024.0 | -13.8% |
| 9/09 | 869.5 | 1,034.5 | -16.0% |
| 10/09 | 857.7 | 1,044.3 | -17.9% |
| 11/09 | 831.9 | 726.4 | 14.5% |
| 12/09 | 774.8 | 732.6 | 5.8% |

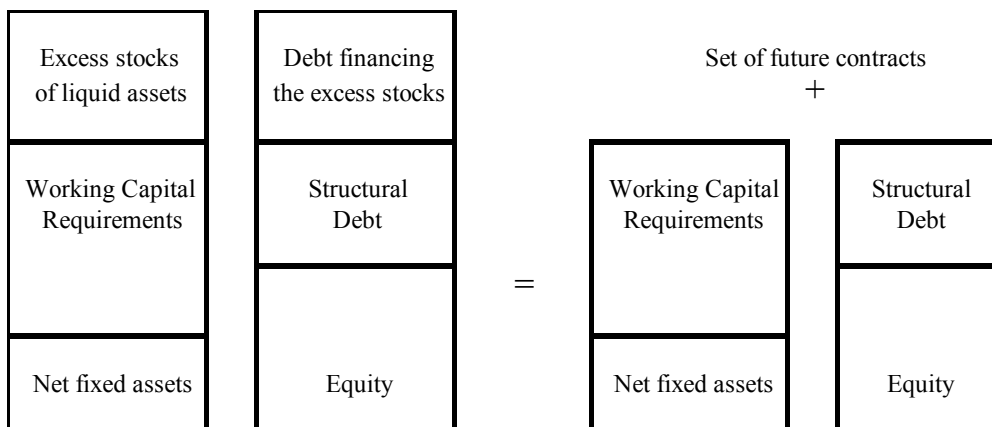
6. Valuation when the inventories are a liquid commodity

Now, let's take a closer look at Russoil and consider the fact that the inventories of the company are sunflower seeds, a very liquid commodity. If the inventories are a very liquid commodity, then it is not correct to treat the excess inventories as working capital requirements. We call excess inventories to those over a minimum or safety inventory (may be defined as the amount needed during the period in which new inventories may be supplied). For example, in the case of Russoil, we call excess inventories to those over a month of sales.

A company like Russoil could maintain its minimum inventory and buy futures contracts to ensure the future supply of seeds⁵. In that case, the company would have a much lower amount of inventories and would buy the seeds in the future months at the future price (spot plus cost of carry). The cost of carry incorporates the financial interest plus the storage costs. This company will be identical in terms of risk to Russoil. The only difference is that Russoil buys all of its annual needs of seeds in December. But we also know that to buy futures contracts on seeds is identical to buy the seeds borrowing money, and that is what Russoil does: buys the seeds in December borrowing money. It is represented on Figure 7.

Figure 7. Equivalence of excess liquid stocks financed with debt to a set of future contracts.

If the excess stock is a very liquid commodity, then, for valuation purposes, it is not correct to treat the excess inventories as working capital requirements



Note that for Russoil we have also considered the cost of carry: the financial expenses are the interest on the bank debt, and the storage costs that are included in the general expenses. Then, a correct valuation of Russoil should consider the interest due to financing the excess seeds and their storage costs in the same way, as operating expenses, and the debt that finances the excess inventories as part of the working capital requirements.

Table 20 contains the correct balance sheets of Russoil for valuation purposes. The inventories are split into “minimum inventory” (line 2) and “excess inventory” (line 3). Analogously, the financial debt is split into “Debt financing excess liquid inventories” (line 6, equal to the “excess inventory”) and “Structural Debt” (line 7). Note that the “excess inventory” financed with the “Debt financing excess liquid inventories” is equal to a group of future contracts on seeds. In that

⁵ Or to enter into an agreement with a seed supplier to cover its future needs.

case the structural debt is negative, which means that if the minimum inventory is one month of sales, the Russoil is an unlevered company.

Table 21 contains the calculation of the free cash flows of Russoil if the excess inventories are liquid assets. Note that table 21 has two changes with respect to table 2: The interest paid on the debt that finances the excess seeds is now deducted, and the increase of Working Capital Requirements now consider only the "minimum inventory". Note that the Equity cash flows are identical on tables 2 and 21.

Table 22 contains the valuation results of Russoil in November and December 2003. Table 23 measures the error of not considering the seeds as liquid assets when they are liquid. The undervaluation ranges between 12% and 14%.

We have pointed out that Equity Cash Flows are equal on table 2 (not considering the seeds as liquid assets) and on table 21 (considering the seeds as liquid assets). The undervaluation is due to the required return to equity (K_e). On figure 3 it may be seen that if we consider the excess inventory as working capital requirements, then the total debt is considered as structural debt and the required return to equity (K_e) is higher than K_u on all months except on November, when the total debt is zero. The average K_e on Figure 3 is 1.16%, while K_u is 0.85%. The relation between K_e and K_u is formula (6):

$$K_e = K_u + \frac{D(1-T)}{E}(K_u - K_d) \quad (6)$$

If we consider the seeds as liquid assets, the structural debt of Russoil is zero all months and, therefore, and the required return to equity (K_e) is equal to K_u on all months.

Table 20. Balance sheet of Russoil considering seeds as liquid assets

| line | | 11/03 | 12/03 | 1/04 | 2/04 | 3/04 | 4/04 | 5/04 | 6/04 | 7/04 | 8/04 | 9/04 | 10/04 | 11/04 | 12/04 |
|------|--|------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|------------|------------|------------|--------------|
| 1 | Cash | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 | 140 |
| 2 | Minimum stock | 201 | 203 | 205 | 207 | 209 | 211 | 213 | 215 | 217 | 220 | 222 | 224 | 226 | 229 |
| 3 | Excess stock | 0 | 2,370 | 2,165 | 1,958 | 1,749 | 1,538 | 1,325 | 1,109 | 892 | 672 | 450 | 226 | 0 | 2,670 |
| 4 | Fixed assets | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 5 | Total assets | 341 | 2,712 | 2,510 | 2,305 | 2,098 | 1,889 | 1,678 | 1,465 | 1,249 | 1,032 | 812 | 590 | 366 | 3,039 |
| 6 | Debt financing excess liquid inventories | 0 | 2,370 | 2,165 | 1,958 | 1,749 | 1,538 | 1,325 | 1,109 | 892 | 672 | 450 | 226 | 0 | 2,670 |
| 7 | Structural Debt | 0 | -16 | -25 | -35 | -46 | -58 | -70 | -83 | -97 | -112 | -128 | -145 | 0 | -18 |
| 8 | Equity | 341 | 359 | 370 | 382 | 395 | 409 | 423 | 439 | 455 | 472 | 490 | 509 | 366 | 387 |
| 9 | Total | 341 | 2,712 | 2,510 | 2,305 | 2,098 | 1,889 | 1,678 | 1,465 | 1,249 | 1,032 | 812 | 590 | 366 | 3,039 |

Table 21. Monthly free cash flows of Russoil considering seeds as liquid assets

| | 12/03 | 1/04 | 2/04 | 3/04 | 4/04 | 5/04 | 6/04 | 7/04 | 8/04 | 9/04 | 10/04 | 11/04 | 12/04 |
|----------------------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|--------------|------------|
| Gross margin | 83.7 | 84.5 | 85.4 | 86.2 | 87.1 | 87.9 | 88.8 | 89.7 | 90.6 | 91.5 | 92.4 | 93.4 | 94.3 |
| - general expenses | -53.6 | -54.1 | -54.6 | -55.2 | -55.7 | -56.3 | -56.8 | -57.4 | -58.0 | -58.6 | -59.2 | -59.7 | -60.3 |
| - interest on excess seeds | 0.0 | -11.8 | -10.7 | -9.6 | -8.5 | -7.4 | -6.3 | -5.1 | -4.0 | -2.8 | -1.6 | -0.4 | 0.0 |
| NOPBT | 30.1 | 18.7 | 20.0 | 21.4 | 22.8 | 24.3 | 25.7 | 27.2 | 28.6 | 30.1 | 31.7 | 33.2 | 33.9 |
| taxes on NOPBT | -12.0 | -7.5 | -8.0 | -8.6 | -9.1 | -9.7 | -10.3 | -10.9 | -11.5 | -12.1 | -12.7 | -13.3 | -13.6 |
| NOPAT | 18.1 | 11.2 | 12.0 | 12.9 | 13.7 | 14.6 | 15.4 | 16.3 | 17.2 | 18.1 | 19.0 | 19.9 | 20.4 |
| - increase of WCR | -18.1 | -11.2 | -12.0 | -12.9 | -13.7 | -14.6 | -15.4 | -16.3 | -17.2 | -18.1 | -19.0 | 142.9 | -20.4 |
| FCF = ECF | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 162.8 | 0.0 |

Table 22. Valuation of Russoil using APV with monthly data, considering seeds as liquid assets

| | 11/03 | 12/03 |
|-----------------------|---------|---------|
| Ku | 0.85% | 0.85% |
| Vu = PV (Ku; FCF) | 1,355.6 | 1,367.1 |
| VTS = PV (Ku; D T Ku) | 0.0 | 0.0 |
| E + D = VTS + Vu | 1,355.6 | 1,367.1 |
| E = (E+D) - D | 1,355.6 | 1,367.1 |

Table 23. Valuation of Russoil using APV with monthly data. Error of not considering the seeds as liquid assets, when they are

| | Equity value (E) considering the seeds as liquid assets | Equity value (E) not considering the seeds as liquid assets | error |
|-------|---|---|--------|
| 11/03 | 1,355.6 | 1,166.0 | -14.0% |
| 12/03 | 1,367.1 | 1,175.9 | -14.0% |
| 1/04 | 1,378.7 | 1,190.8 | -13.6% |
| 2/04 | 1,390.5 | 1,205.4 | -13.3% |
| 3/04 | 1,402.3 | 1,219.7 | -13.0% |
| 4/04 | 1,414.2 | 1,233.7 | -12.8% |
| 5/04 | 1,426.2 | 1,247.3 | -12.5% |
| 6/04 | 1,438.3 | 1,260.5 | -12.4% |
| 7/04 | 1,450.6 | 1,273.4 | -12.2% |
| 8/04 | 1,462.9 | 1,285.9 | -12.1% |
| 9/04 | 1,475.3 | 1,298.0 | -12.0% |
| 10/04 | 1,487.9 | 1,309.7 | -12.0% |
| 11/04 | 1,337.7 | 1,158.1 | -13.4% |
| 12/04 | 1,349.0 | 1,168.0 | -13.4% |
| 1/05 | 1,360.5 | 1,183.5 | -13.0% |

7. Conclusions

The correct way of valuing seasonal companies by cash flow discounting is to use monthly data. If we use annual data, some adjustments are needed.

We have shown that when using annual data in the context of the adjusted present value (APV), the value of the unlevered equity (V_u) and the value of the tax shields (VTS) calculations must be adjusted. However, the debt that we have to subtract to calculate the equity value needs not to be adjusted.

Errors due to using annual data without doing the adjustments are big. We have shown that the equity value calculated using annual data without doing the adjustments understates the true value in a 45% if the valuation is done at the end of December, and overstates the true value in a 38% if the valuation is done at the end of November.

Valuing a seasonal company using annual data, average debt and average working capital requirements is not a good approximation: the error ranges from – 17.9% to 8.5%.

When the inventories are a liquid commodity such as grain or seeds, it is not correct to consider all of them as working capital requirements. The excess inventories financed with debt are equivalent to a set of futures contracts. We have shown that not considering it undervalues the company.

APPENDIX 1

| Month | Free cash flow | Present value | Year | Free cash flow | Present value |
|-------|-------------------|---------------------------------|------|----------------|-------------------------------------|
| 1 | FCF_1 | $FCF_1 / (1+Ku)$ | | | |
| 2 | $FCF_1(1+g)$ | $FCF_1(1+g) / (1+Ku)^2$ | | | |
| 3 | $FCF_1(1+g)^2$ | $FCF_1(1+g)^2 / (1+Ku)^3$ | | | |
| 4 | $FCF_1(1+g)^3$ | $FCF_1(1+g)^3 / (1+Ku)^4$ | | | |
| 5 | $FCF_1(1+g)^4$ | $FCF_1(1+g)^4 / (1+Ku)^5$ | | | |
| 6 | $FCF_1(1+g)^5$ | $FCF_1(1+g)^5 / (1+Ku)^6$ | | | |
| 7 | $FCF_1(1+g)^6$ | $FCF_1(1+g)^6 / (1+Ku)^7$ | | | |
| 8 | $FCF_1(1+g)^7$ | $FCF_1(1+g)^7 / (1+Ku)^8$ | | | |
| 9 | $FCF_1(1+g)^8$ | $FCF_1(1+g)^8 / (1+Ku)^9$ | | | |
| 10 | $FCF_1(1+g)^9$ | $FCF_1(1+g)^9 / (1+Ku)^{10}$ | | | |
| 11 | $FCF_1(1+g)^{10}$ | $FCF_1(1+g)^{10} / (1+Ku)^{11}$ | | | |
| 12 | $FCF_1(1+g)^{11}$ | $FCF_1(1+g)^{11} / (1+Ku)^{12}$ | 1 | Sum of FCF | Sum of FCF / (1+ Ku _{ae}) |
| Sum | Sum of FCF | Sum of PV (FCF) | Sum | Sum of FCF | Sum of FCF / (1+ Ku _{ae}) |

The sum of the 12 monthly FCFs is:

$$\text{Sum of FCF} = (FCF_1 / g) [(1+g)^{12} - 1].$$

If $g = 0$, then the Sum of FCF = 12 FCF₁

The sum of the Present Values of the 12 monthly FCFs is:

$$\text{Sum of PV (FCF)} = [\text{FCF1} / (\text{g} - \text{Ku})] [((1+\text{g})/(1+\text{Ku}))^{12} - 1].$$

If $\text{g} = 0$, then the Sum of PV (FCF) = $(\text{FCF1} / \text{Ku}) [1 - 1/(1+\text{Ku})^{12}]$

If $\text{g} = \text{Ku}$, then the Sum of PV (FCF) = $12 \text{ FCF1} / (1+\text{Ku})$

To perform a correct valuation, the sum of the present values of the monthly Free Cash Flows should be equal to the present value of the annual Free Cash Flow. The annual free cash flow is the sum of the 12 monthly Free Cash Flows:

$$[\text{FCF1} / (\text{g} - \text{Ku})] [((1+\text{g})/(1+\text{Ku}))^{12} - 1] = (\text{FCF1} / \text{g}) [(1+\text{g})^{12} - 1] / (1 + \text{Kuae})$$

$$\text{Kuae} = \frac{[(1 + \text{g})^{12} - 1] (\text{g} - \text{Ku})}{\text{g} \left[\left(\frac{1 + \text{g}}{1 + \text{Ku}} \right)^{12} - 1 \right]} - 1$$

$$\text{If } \text{g} = 0, \text{ then } \text{Kuae} = \frac{12 \text{ Ku}}{1 - \frac{1}{(1 + \text{Ku})^{12}}} - 1 > (1 + \text{Ku})^6 - 1$$

$$\text{If } \text{g} = \text{Ku}, \text{ then } \text{Kuae} = [(1 + \text{g})^{12} - 1] (1 + \text{g}) / (12 \text{ g})$$

Table A.1 has the magnitude of Kuae for different values of g and Ku . It may be seen that $\text{Kuae} > (1 + \text{Ku})^6 - 1$ if $\text{g} > -3\%$.

Table A.1. Kuae as a function of g and Ku

| | | Ku | | | | | | | |
|----------------------------|-------|-------|-------|-------|-------|-------|-------|--------|--------|
| | | 0.4% | 0.6% | 0.8% | 1.0% | 1.2% | 1.4% | 1.6% | 2.0% |
| g | -4.0% | 2.42% | 3.64% | 4.87% | 6.11% | 7.35% | 8.60% | 9.86% | 12.39% |
| | -3.0% | 2.47% | 3.72% | 4.97% | 6.24% | 7.51% | 8.78% | 10.07% | 12.66% |
| | -2.0% | 2.52% | 3.79% | 5.07% | 6.36% | 7.66% | 8.97% | 10.28% | 12.93% |
| | -1.0% | 2.57% | 3.87% | 5.18% | 6.49% | 7.82% | 9.15% | 10.49% | 13.20% |
| | 0.0% | 2.62% | 3.94% | 5.28% | 6.62% | 7.97% | 9.33% | 10.70% | 13.47% |
| | 1.0% | 2.67% | 4.02% | 5.38% | 6.74% | 8.12% | 9.51% | 10.91% | 13.74% |
| | 2.0% | 2.72% | 4.09% | 5.47% | 6.87% | 8.27% | 9.69% | 11.12% | 14.00% |
| $(1 + \text{Ku})^6 - 1$ | | 2.42% | 3.65% | 4.90% | 6.15% | 7.42% | 8.70% | 9.99% | 12.62% |
| $(1 + \text{Ku})^{12} - 1$ | | 4.9% | 7.4% | 10.0% | 12.7% | 15.4% | 18.2% | 21.0% | 26.8% |

In the case of Russoil, as $\text{Ku} = 0.85\%$ and $\text{g} = 1\%$ until December 2008, $\text{Kuae} = 5.716754752\%$.

APPENDIX 2

| Month | Free cash flow | Present value | Year | Free cash flow | Present value |
|-------|----------------|--------------------------------|------|----------------|----------------------|
| 1 | | | | | |
| 2 | | | | | |
| 3 | | | | | |
| 4 | Purchase | Purchase / (1+Ku) ⁴ | | | |
| 5 | | | | | |
| 6 | | | | | |
| 7 | | | | | |
| 8 | | | | | |
| 9 | | | | | |
| 10 | | | | | |
| 11 | | | | | |
| 12 | | | 1 | Purchase | Purchase / (1+ Kuas) |
| Sum | Purchase | Purchase / (1+Ku) ⁴ | Sum | Purchase | Purchase / (1+ Kuas) |

The Present Value of the Purchase in month n, using monthly data is:

$$PV (\text{Purchase}) = \text{Purchase} / (1+Ku)^n$$

To perform a correct valuation, the Present Value of the Purchase in month n, using monthly data should be equal to the present value of the annual Free Cash Flow (considering the purchase at the end of the year):

$$\text{Purchase} / (1+Ku)^n = \text{Purchase} / (1+ Kuas)$$

$$Kuas = (1+Ku)^{n-1}$$

Table A.2. Kuas as a function of n and Ku

| | | Ku | | | | | | | | |
|---|----|-------|-------|--------|--------|--------|--------|--------|--------|--------|
| | | 0.4% | 0.6% | 0.8% | 1.0% | 1.2% | 1.4% | 1.6% | 1.8% | 2.0% |
| n | 1 | 0.40% | 0.60% | 0.80% | 1.00% | 1.20% | 1.40% | 1.60% | 1.80% | 2.00% |
| | 2 | 0.80% | 1.20% | 1.61% | 2.01% | 2.41% | 2.82% | 3.23% | 3.63% | 4.04% |
| | 3 | 1.20% | 1.81% | 2.42% | 3.03% | 3.64% | 4.26% | 4.88% | 5.50% | 6.12% |
| | 4 | 1.61% | 2.42% | 3.24% | 4.06% | 4.89% | 5.72% | 6.56% | 7.40% | 8.24% |
| | 5 | 2.02% | 3.04% | 4.06% | 5.10% | 6.15% | 7.20% | 8.26% | 9.33% | 10.41% |
| | 6 | 2.42% | 3.65% | 4.90% | 6.15% | 7.42% | 8.70% | 9.99% | 11.30% | 12.62% |
| | 7 | 2.83% | 4.28% | 5.74% | 7.21% | 8.71% | 10.22% | 11.75% | 13.30% | 14.87% |
| | 8 | 3.25% | 4.90% | 6.58% | 8.29% | 10.01% | 11.76% | 13.54% | 15.34% | 17.17% |
| | 9 | 3.66% | 5.53% | 7.43% | 9.37% | 11.33% | 13.33% | 15.36% | 17.42% | 19.51% |
| | 10 | 4.07% | 6.16% | 8.29% | 10.46% | 12.67% | 14.92% | 17.20% | 19.53% | 21.90% |
| | 11 | 4.49% | 6.80% | 9.16% | 11.57% | 14.02% | 16.52% | 19.08% | 21.68% | 24.34% |
| | 12 | 4.91% | 7.44% | 10.03% | 12.68% | 15.39% | 18.16% | 20.98% | 23.87% | 26.82% |

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